## Advanced Training Strategies: Pyramid Search

Genetic Programming

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Normal Graph

Best Fitness


Premature convergence


## Idea:

- Run many independent GP runs at the same time (in Parallel)
- Compare fittest individuals between the program's populations
- Prunes least fit populations
- No sharing of individuals between populations



## Pseudo Code



1 def pyramid(num_pops, pop_size, prune_ratio, num_gen, max_generations)\{ 2 popsleft = num_pops
3 while(not solved and popsleft != 1 and generations < max_generations)\{
4 evolve_pops(pop_size, num_gen)
5 remove_least_fit_pops(round(popleft * prune_ratio))
$6 \quad$ popsleft $=$ popsleft - round(popleft * prune_ratio)
generations += num_gen
\}
9 \}


## Pros of Pyramid Search

- Great for large scale problems or if the problems have a complex fitness landscapes with multiple local optima
- It is faster than running multiple vanilla GP runs because it prunes out worst fit runs



## Cons of Pyramid Search

- There are now more parameters to consider and to optimize
- Pyramid Search has to maintain multiple runs so it increases the memory demand
- Depends on setup and intention, running the same number of subpopulations, pyramid search uses less memory vs running all to completion rive
Pent Pyramid search's increased memory requirements comes from having to run many subpopulations at the same time.


## Pyramid Search vs normal paper comparison

Pyramid search has high probability of success with fewer evaluations
"total evaluations" typically refers to the total number of fitness evaluations performed during the execution of the algorithm.

| Methods | Num Suc | Mean | SD. |
| :--- | ---: | ---: | ---: |
| Norm49 | 81 | 21740 | 30838 |
| Norm490 | 97 | 24361 | 16870 |
| Pyr-ps49-np10-pr0.1 | 100 | 11253 | 1675 |
| Pyr-ps49-np10-pr0.2 | 99 | 7961 | 1194 |
| Pyr-ps49-np10-pr0.5 | 94 | 6885 | 11099 |

Table 1: Mean and Standard Deviation, Number of Evaluations to First Solution, Max Problem


| Methods | Runs | Total Evals |
| :--- | :--- | :--- |
| Pyr-ps49-np-100-pr0.2 | 4 for $27 \times 49,000$ | $108 \times 49,000$ |
| Pyr-ps49-np-100-pr0.5 | 7 for $17 \times 49,000$ | $119 \times 49,000$ |
| Pyr-ps49-np-10-pr0.1 | 8 for $15 \times 49,000$ | $120 \times 49,000$ |
| Pyr-ps 490 -np-10-pr0.1 | 5 for $26 \times 49,000$ | $130 \times 49,000$ |
| Pyr-ps490-np-10-pr0.5 | 8 for $17 \times 49,000$ | $136 \times 49,000$ |
| Pyr-ps49-np-10-pr0.5 | 35 for $4 \times 4,9000$ | $140 \times 4,9000$ |
| Pyr-ps49-np-100-pr0.1 | 3 for $48 \times 49,000$ | $144 \times 49,000$ |
| Pyr-ps490-np-10-pr0.2 | 7 for $23 \times 49,000$ | $161 \times 49,000$ |
| Norm4900 | 7 for $23 \times 49,000$ | $161 \times 49,000$ |
| Norm49 | 32 for $7 \times 49,000$ | $224 \times 49,000$ |
| Pyr-ps49-np-10-pr0.2 | 7 for $45 \times 49,000$ | $315 \times 49,000$ |
| Norm490 | 7 for $46 \times 49,000$ | $322 \times 49,000$ |

## WE IMPLEMENTED IT!!!!

The parameters the paper used
Variables
num_pop = 10 pop_size $=50$ prune_ratio = 0.2
num_gen = 10
max_generations: 100

Before we implemented it we were looking for a speedup, an improvement in premature convergence,
overall fitness results and memory consumption

## Assignment 1 Part B

- Assignment 1 part B also suffered from premature convergence

Mean Fitness Per Generation
Best Fitness Per Generation
10 Runs, Normal, 800 PopSize


10 Runs, Normal, 800 PopSize


## Assignment 1 Part B Cont.

- Average Execution Time 6.786 Seconds

| Testing Set |  |  |  |
| :---: | :---: | :---: | :---: |
| TARGET <br> OUTPUT | Cammeo | Osmancik | SUM |
| Cammeo | $\begin{gathered} 945 \\ 33.65 \% \end{gathered}$ | $\begin{gathered} 370 \\ 13.18 \% \end{gathered}$ | $\begin{gathered} 1315 \\ 71.86 \% \\ 28.14 \% \end{gathered}$ |
| Osmancik | $\begin{gathered} 183 \\ 6.52 \% \end{gathered}$ | $\begin{gathered} 1310 \\ 46.65 \% \end{gathered}$ | $\begin{gathered} 1493 \\ 87.74 \% \\ 12.26 \% \end{gathered}$ |
| SUM | 1128 83.78\% 16.22\% | $\begin{gathered} 1680 \\ 77.98 \% \\ \text { 22.02\% } \end{gathered}$ | $\begin{gathered} 2255 \text { / } 2808 \\ 80.31 \% \\ 19.69 \% \end{gathered}$ |



## Applying Pyramid Search To Assignment 1

- Using 10 sub-populations, a prune ratio of 0.2 and 10 generations between pruning

Mean Fitness Per Generation
10 Runs, Pyramid, 800 PopSize


Best Fitness Per Generation
10 Runs, Pyramid, 800 PopSize


## Applying Pyramid Search To Assignment 1 Cont.

- Average Execution Time 4.6055 Seconds

| Testing Set |  |  |  |
| :---: | :---: | :---: | :---: |
| TARGET <br> OUTPUT | Cammeo | Osmancik | SUM |
| Cammeo | $\begin{gathered} 1022 \\ 36.37 \% \end{gathered}$ | $\begin{gathered} 121 \\ 4.31 \% \end{gathered}$ | $\begin{gathered} 1143 \\ 89.41 \% \\ 10.59 \% \end{gathered}$ |
| Osmancik | $\begin{gathered} 104 \\ 3.70 \% \end{gathered}$ | $\begin{gathered} 1563 \\ 55.62 \% \end{gathered}$ | $\begin{gathered} 1667 \\ 93.76 \% \\ 6.24 \% \end{gathered}$ |
| SUM | $\begin{gathered} 1126 \\ 90.76 \% \\ 9.24 \% \end{gathered}$ | $\begin{gathered} 1684 \\ 92.81 \% \\ 7.19 \% \end{gathered}$ | $\begin{gathered} 2585 \text { / } 2810 \\ 91.99 \% \\ 8.01 \% \end{gathered}$ |
| Before it w as 80.31\% |  |  |  |

Memory Usage Of Assignment 1 Part B (Pyramid)
10 Runs, 800 PopSize


## Conclusions

- Running pyramid search gave better results on average in less time
- According to our tests we did not reduce premature convergence or increase genetic diversity of our populations
- Peak memory usage was less than running 10 subpopulations without with pyramid search


## References

[1] Ciesielski, V., \& Li, X. (2003). Pyramid search: finding solutions for deceptive problems quickly in genetic programming. CEC: 2003 CONGRESS ON EVOLUTIONARY COMPUTATION, VOLS 1-4, PROCEEDINGS, 2, 936-943 Vol.2. https://doi.org/10.1109/CEC.2003.1299767
[2] Rice (Cammeo and Osmancik). (2019). UCI Machine Learning Repository. https://doi.org/10.24432/C5MW4Z.
[3] Poli, Riccardo, et al. A Field Guide to Genetic Programming. Lulu Press, 2008.

## The MAX Problem from the Paper

Goal is to find maximum value for a given depth using a GP with a function set of $\{x,+\}$ and terminals of $\{0.5\}$

## Desired solution is a full tree with 0.5 on all terminals

## This problem which was presented in the paper is known as a "deceptive

 problem" that "displays obvious premature convergence behaviour"